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Block Graphs in Practice

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Abstract

Motivated by the rapidly increasing size of genomic databases, code repositories and versioned texts, several compression schemes have been proposed that work well on highly-repetitive strings and also support fast random access: e.g., LZ-End, RLZ, GDC, augmented SLPs, and block graphs. Block graphs have good worst-case bounds but it has been an open question whether they are practical. We describe an implementation of block graphs that, for several standard datasets, provides better compression and faster random access than competing schemes.

1 Introduction

Advances in DNA sequencing technology have led to massive genomic databases, the open-source movement has led to massive code repositories, and the popularity of wikis has led to massive versioned textual databases. Fortunately, all these datasets tend to be highly repetitive and, thus, highly compressible. Compressing them is only useful, however, if we can still access them quickly afterwards. Although many papers have been published about compression schemes with fast random access (see [6] for a recent survey), most have been about schemes such as Huffman coding, LZ78, CSAs or BWT-based coding. Only relatively recently have researchers started proposing schemes with random access and LZ77-like compression, which is better suited to highly-repetitive strings.

One approach uses variants of LZ77 itself. Kreft and Navarro's LZ-End [7] is practical but lacks good worst-case bounds, for both the compression and the random-access time. Kuruppu, Puglisi and Zobel's Relative Lempel-Ziv (RLZ) [8, 9] or Deorowicz and Grabowski's Genome Differential Compressor (GDC) [4] are also practical but are not general-purpose: we can apply them only when we have a good reference sequence, or can construct one. Even then, Deorowicz, Danek and

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returns the number of occurrences of b before position i in B and $select_b(B, i)$ returns the position of the i th b in B . Efficient data structures supporting these operations have been extensively studied (see, e.g., [11, 12]).

Recall, each level of the block graph consists of a number of nodes, either internal nodes, or leaves. Let B_d be a bitvector which indicates whether the i th node (from the left) at depth d is a leaf, $B_d[i] = 0$, or an internal node, $B_d[i] = 1$. We define another bitvector R_d , where $R_d[i] = 1$ if and only if $B_d[i] = 1$ and $B_d[i + 1] = 1$ for $i < n - 1$. That is, we mark a 1 bit for each instance of two adjacent internal nodes in B_d , otherwise $R_d[i] = 0$. Let L_d be an array that holds leaf nodes at depth d . The structure of a leaf node is discussed below. Finally, let T be the concatenation of the textual representation (ie. the corresponding substrings) of all internal nodes at the truncated depth, d' . As adjacent text blocks share $2^{\log n - d' - 1}$ characters, we concatenate only the last half of a new adjacent block to T . Non-adjacent blocks are fully concatenated. We utilize an R_d bitvector at this level; however, we mark $R_d[i] = 1$ if the i th node at the truncated depth is a text block.

Navigating the block graph

The main operation is to traverse from an internal node to one of its three children. Say we are currently at the j th internal node at depth d of the block graph — that is, we are at $B_d[i]$, where $i = select_1(B_d, j)$. Each internal node has three children. If these children were independent then locating the left child of the current node would be simply three times the node's position on its level, that is $3j = 3 \cdot rank_1(B_d, i)$. However, in a block graph, adjacent internal nodes share exactly one child, so we correct for this by subtracting the number of adjacent internal nodes at this depth prior to the current node — this is given by $rank_1(R_d, i)$. To find the position corresponding to the left child of a node in B_{d+1} we compute $leftchild(B_d, i) = 3 \cdot rank_1(B_d, i) - rank_1(R_d, i)$.

Given the address of the left child it is easy to find the center or right child by adding 1 or 2, respectively. If $B_d[i] = 0$ then we are at a leaf node, and its leaf information is at $L_d[rank_0(B_d, i)]$. Once we reach the truncated depth we access the text of an internal node by computing its offset in T as $T[(rank_1(B_d, i) \cdot 2^{\log n - d' - 1}) - (rank_1(R_d, i) \cdot 2^{\log n - d' - 1})]$.

Leaf nodes

In a block graph, leaves point to internal nodes. For each leaf we store two values, the position of the destination node on the current level, and an offset in the destination node pointing to the beginning of the leaf block. Note that we do not need to store the depth of the destination node. It is, by definition, on the level above the leaf, and we know this by keeping keep track of the depth during each step in a traversal. To improve compression we store leaf positions and offsets in two separate arrays. At depth d there are no more than $2^{d+1} - 1$ possible nodes, so we can store each position in $\log(2^{d+1} - 1)$ bits. Given that the length of a node at depth d is $b = 2^{\lceil \log n \rceil - d}$ and leaf nodes point to an internal node on the level above, we store each offset in $\log(2^{\lceil \log n \rceil - d - 1})$ bits.

Table 1: Size in MB of repetitive corpus files encoded with ASCII, `gzip`, `xz`, LZ-End and block graphs truncated at text length 4, 8, 16 and 32.

Collection	ASCII	GZIP	XZ	LZ-End	Bg4	Bg8	Bg16	Bg32
world_leaders	49	8.28	0.51	4.52	6.62	5.83	5.72	6.37
Escherichia_Coli	112	31.53	5.18	49.10	49.70	49.57	45.33	46.91
influenza	154	10.63	1.59	21.50	33.16	32.97	33.32	37.89
coreutils	205	49.92	3.70	35.88	42.80	33.19	30.43	33.00
kernel	257	69.39	2.07	19.34	21.21	15.69	13.84	14.05
para	429	116.07	6.09	57.41	72.39	72.13	67.84	70.66
cere	461	120.08	5.07	41.34	57.68	57.54	54.59	57.96
einstein.en.txt	467	163.66	0.33	2.24	3.52	3.07	3.01	3.19

4 Experiments

We have developed an implementation of block graphs¹ and tested it on texts from the Pizza-Chili Repetitive Corpus², a standard testbed for data structures designed for repetitive strings.

We compared compression achieved by the block graph to the LZ-End data structure by Kreft and Navarro [7], and to the general-purpose compressors `gzip` and `xz`; the results are shown in Table 1. `gzip` and `xz` were run with their highest compression setting `-9`, while LZ-End was executed with its default settings. Throughout our experiments we tested block graphs that were truncated such that the smallest blocks were 4, 8, 16 and 32 bytes. Note that `gzip` and `xz` provide compression only, not random access, and are included as reference points for achievable compression. We did not test extraction from bookmarks because Kreft and Navarro’s data structure does not support it (nor does any other implemented data structure).

We then compared how quickly block graphs and LZ-End support extracting substrings of various lengths; the results are shown in Figure 2. The mean extraction speed with LZ-End never exceeded 9 million characters per second while, for sufficiently long extractions from the `kernel` file, the mean extraction speed with the block graph was over 480 million characters per second. Each run of extractions was performed across 10,000 randomly-generated queries. Experiments were conducted on an Intel Core i7-2600 3.4 GHz processor with 8GB of main memory, running Linux 3.3.4; code was compiled with GCC version 4.7.0 targeting `x86_64` with full optimizations. Caches were dropped between runs with `sync && echo 1 > /proc/sys/vm/drop_caches`.

Although `xz` achieves much better compression, block graphs achieve better compression than `gzip` except on the `Escherichia Coli` and `influenza` files. Most importantly, our experiments show that block graphs generally achieve compression comparable to that achieved by LZ-End while supporting significantly faster substring extraction.

¹Available at <http://www.github.com/choobin/block-graph>

²<http://pizzachili.dcc.uchile.cl/repcorpus.html>

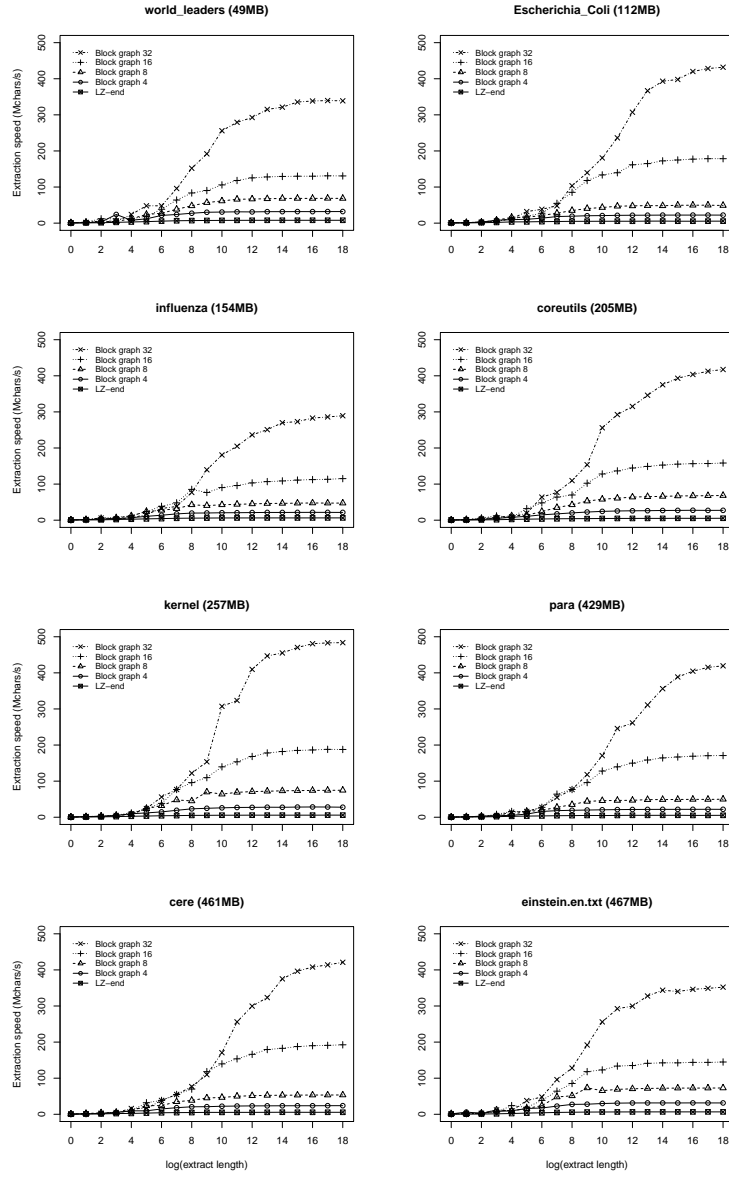


Figure 2: Extraction speeds in millions of characters per second versus the binary logarithm of the length of the extracted substring. Each data point is averaged over 10,000 random substring extractions.

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